

Sage Quick Reference (Basic Math)

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Aim: map standard math notation to Sage commands

Notebook (and commandline)

Evaluate cell: `<shift-enter>`

`com(tab)` tries to complete *command*

`command?(tab)` shows documentation

`command??(tab)` shows source

`a.(tab)` shows all methods for object `a` (more: `dir(a)`)

`search_doc('string or regexp')` shows links to docs

`search_src('string or regexp')` shows links to source

`lprint()` toggle L^AT_EX output mode

`version()` print version of Sage

Insert cell: click on blue line between cells

Delete cell: delete content then backspace

Numerical types

Integers: `Z = ZZ` e.g. `-2 -1 0 1 10^100`

Rationals: `Q = QQ` e.g. `1/2 1/1000 314/100 -42`

Decimals: `R = RR` e.g. `.5 0.001 3.14 -42`

Complex: `C = CC` e.g. `1+i 2.5-3*i`

Basic constants and functions

Constants: `pi = pi` `e = e` `i = i` `infinity = oo`

Approximate: `pi.n(digits=18)` = 3.14159265358979324

Functions: `sin cos tan sec csc cot sinh cosh tanh sech`

`csch coth log ln exp`

`ab = a*b` $\frac{a}{b} = a/b$ $a^b = a^b$ $\sqrt{x} = \sqrt{x}$

$\sqrt[n]{x} = x^{1/n}$ $|x| = \text{abs}(x)$ $\log_b(x) = \log(x, b)$

Symbolic variables: e.g. `t, u, v, y = var('t u v y')`

Define function: e.g. `f(x) = x^2`

As symbolic function (can integrate, etc): `f(x)=x^2 or`

As Python function: `f=lambda x: x^2 or`

`def f(x): return x^2`

Operations on expressions

`factor(...)` `expand(...)` `(...).simplify(...)`

Symbolic equations: `f(x)==g(x)`

`_` is previous output

`_+a _-a _*a _/a` manipulates equation

Solve $f(x) = g(x)$: `solve(f(x)==g(x), x)`

`solve([f(x)==0, g(x,y)==0], x, y)`

`find_root(f(x), a, b)` find $x \in [a, b]$ s.t. $f(x) \approx 0$

$\sum_{i=k}^n f(i) = \text{sum}([f(i) \text{ for } i \text{ in } [k..n]])$

$\prod_{i=k}^n f(i) = \text{prod}([f(i) \text{ for } i \text{ in } [k..n]])$

Calculus

$\lim_{x \rightarrow a} f(x) = \text{limit}(f(x), x=a)$

$\lim_{x \rightarrow a^-} f(x) = \text{limit}(f(x), x=a, \text{dir}='minus')$

$\lim_{x \rightarrow a^+} f(x) = \text{limit}(f(x), x=a, \text{dir}='plus')$

$\frac{d}{dx}(f(x)) = \text{diff}(f(x), x)$

$\frac{\partial}{\partial x}(f(x, y)) = \text{diff}(f(x, y), x)$

`diff = differentiate = derivative`

$\int f(x) dx = \text{integral}(f(x), x)$

`integral = integrate`

$\int_a^b f(x) dx = \text{integral}(f(x), x, a, b)$

Taylor polynomial, deg n about a : `taylor(f(x), x, a, n)`

2d graphics

`line([(x1,y1), ..., (xn,yn)], options)`

`polygon([(x1,y1), ..., (xn,yn)], options)`

`circle((x,y), r, options)`

`text("txt", (x,y), options)`

options as in `plot.options`,

e.g. `thickness=pixel, rgbcolor=(r,g,b), hue=h,`
where $0 \leq r, b, g, h \leq 1$

use option `figsize=[w, h]` to adjust aspect ratio

`plot(f(x), x_min, x_max, options)`

`parametric_plot((f(t), g(t)), t_min, t_max, options)`

`polar_plot(f(t), t_min, t_max, options)`

combine graphs: `circle((1,1), 1)+line([(0,0), (2,2)])`

`animate(list of graphics objects, options).show(delay=20)`

3d graphics

`line3d([(x1,y1,z1), ..., (xn,yn,zn)], options)`

`sphere((x,y,z), r, options)`

`tetrahedron((x,y,z), size, options)`

`cube((x,y,z), size, options)`

`octahedron((x,y,z), size, options)`

`dodecahedron((x,y,z), size, options)`

`icosahedron((x,y,z), size, options)`

options e.g. `aspect_ratio=[1,1,1] color='red' opacity`

`plot3d(f(x,y), [xb,xe], [yb,ye], options)`

add option `plot_points=[m,n]` or use `plot3d_adaptive`

`parametric_plot3d((f(t), g(t), h(t)), [tb,te], options)`

`parametric_plot3d((f(u,v), g(u,v), h(u,v)), [ub,ue], [vb,ve], options)`

use `+` to combine graphics objects

Discrete math

`[x] = floor(x)` $[x] = \text{ceil}(x)$

Remainder of n divided by k = `n%k` $k|n$ iff `n%k==0`

`n! = factorial(n)` $\binom{x}{m} = \text{binomial}(x, m)$

$\phi = \text{golden_ratio}$ $\phi(n) = \text{euler_phi}(n)$

Strings: e.g. `s = 'Hello' = "Hello" = ""+"He"+'llo'`

`s[0]='H'` $s[-1]='o'$ $s[1:3]='el'$ $s[3:]='lo'$

Lists: e.g. `[1, 'Hello', x] = []+[1, 'Hello']+ [x]`

Tuples: e.g. `(1, 'Hello', x)` (immutable)

Sets: e.g. `{1, 2, 1, a} = Set([1, 2, 1, 'a'])` ($\{1, 2, a\}$)

List comprehension \approx set builder notation, e.g.

$\{f(x) : x \in X, x > 0\} = \text{Set}([f(x) \text{ for } x \text{ in } X \text{ if } x > 0])$

Linear algebra

$\begin{pmatrix} 1 \\ 2 \end{pmatrix} = \text{vector}([1, 2])$

$\begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix} = \text{matrix}([[1, 2], [3, 4]])$

$\begin{vmatrix} 1 & 2 \\ 3 & 4 \end{vmatrix} = \det(\text{matrix}([[1, 2], [3, 4]]))$

$Av = A*v$ $A^{-1} = A^{-1}$ $A^t = A.\text{transpose}()$

methods: `nrows()` `ncols()` `nullity()` `rank()` `trace()`...

Sage modules and packages

`from module_name import *` (many preloaded)

e.g. `calculus` `coding` `combinat` `crypto` `functions` `games`
`geometry` `graphs` `groups` `logic` `matrix` `numerical` `plot`
`probability` `rings` `sets` `stats`

`sage.module_name.all.(tab)` shows exported commands

Std packages: Maxima GP/PARI GAP Singular R Shell...

Opt packages: Biopython Fricas(Axiom) Gnuplot Kash...

`%package_name` then use package command syntax

`time command` to show timing information